

VIVEKANANDA COLLEGE  
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NAAC ACCREDITED 'A' GRADE



Topic: T-S DIAGRAM

Course Title: Chemistry (Gen)

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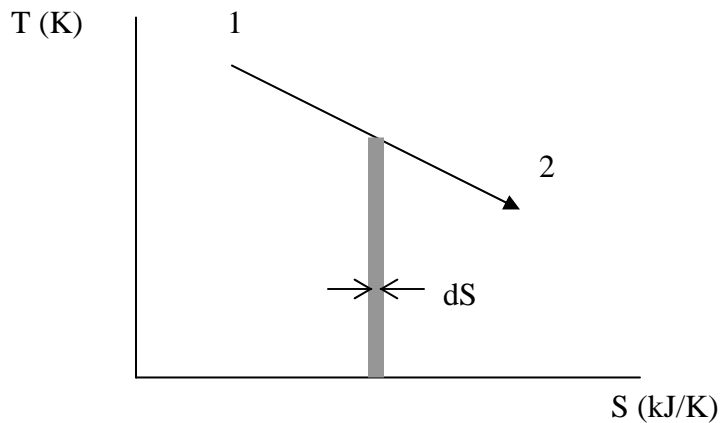
Name of the Department: Chemistry

## THE TEMPERATURE-ENTROPY, T-S, DIAGRAM

Clausius' principle for an internally reversible process:

$$\delta Q = TdS$$

Any process can be graphed on a T-S (or T-s) diagram (just as with T-v or P-v diagrams). Because of Clausius' Principle, the T-S diagrams for internally reversible processes can be used to calculate heat transfer.

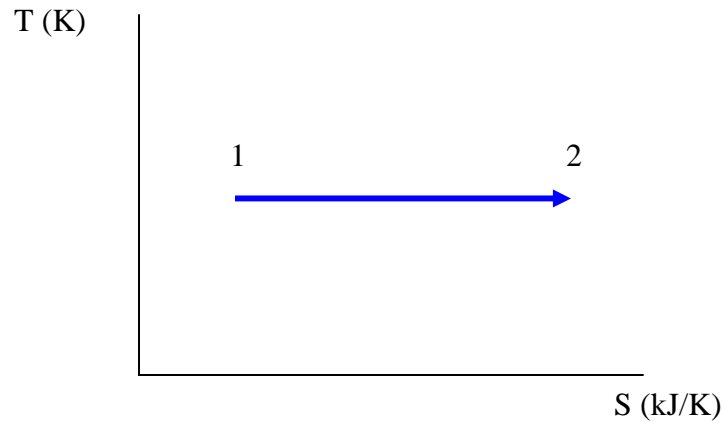


Shaded area =  $TdS = \delta Q$  and the total area under process line for the internally reversible process  $1 \rightarrow 2$  is the heat transferred during the process:

$$\int_1^2 TdS = Q_{1 \rightarrow 2}$$

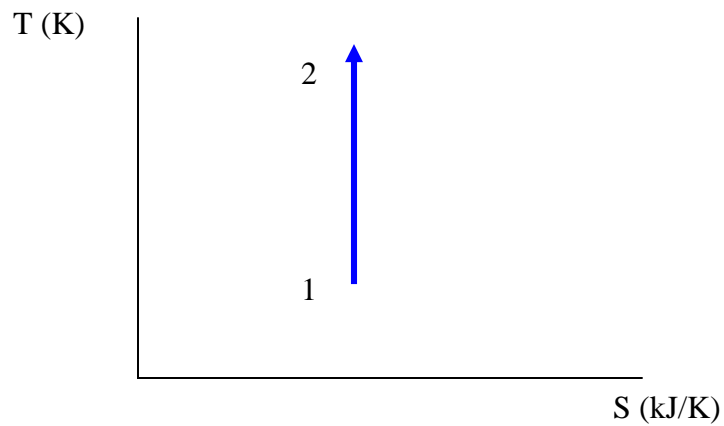
## SPECIAL T-S DIAGRAMS

1. For an isothermal internally reversible process:



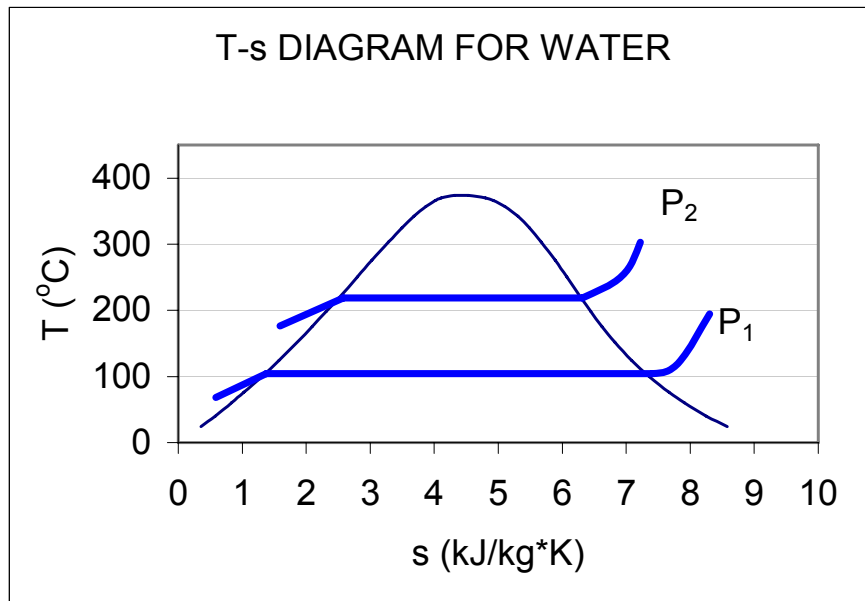
$$Q_{1 \rightarrow 2} = T(S_2 - S_1) =$$

2. For an adiabatic and internally reversible process (isentropic):



$$(S_2 - S_1) = 0$$

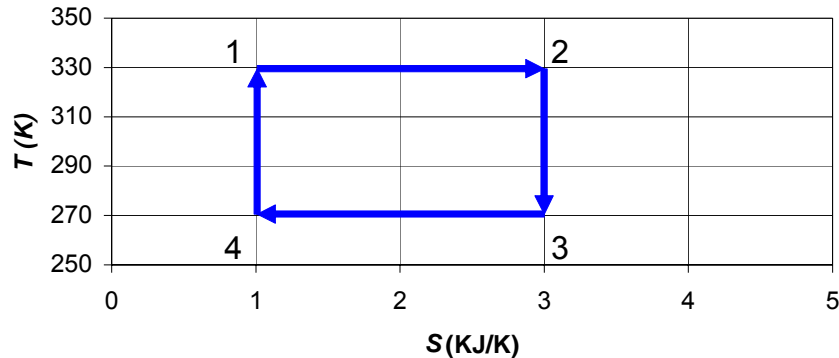
3. For pure substances with liquid vapor phases, the T-s diagram shows similar constant pressure lines as in the P-v and T-v diagrams, indicating vaporization/condensation processes at constant pressure are isothermal and as P increases,  $s_{fg}$  decreases:



where  $P_2 > P_1$ . As with the T-s and P-v diagrams, the critical point (where liquid and vapor phases are indistinguishable) is at the top of the phase curve where the saturated liquid and vapor lines meet. A pure substance is compressed liquid for  $s < s_f$ , superheated vapor for  $s > s_g$ , and a saturated liquid-vapor mixture between the saturated liquid and vapor lines.

#### 4. For Carnot cycles:

##### (a) Carnot Heat Engine – all totally reversible processes



1→2 is isothermal expansion, the heat input process, and  $Q_H = \text{area under line 1-2}$  or  $Q_H = T_1(s_2-s_1)$  (will be positive)

2→3 is isentropic (adiabatic and reversible) expansion, the work output process.  $W_{2\rightarrow3}$  cannot be inferred from the T-S diagram.

3→4 is isothermal compression, the heat rejection process, and  $Q_L = \text{area under line 3-4}$  or  $Q_L = T_3(s_4-s_3)$  (will be negative and  $<Q_H$ )

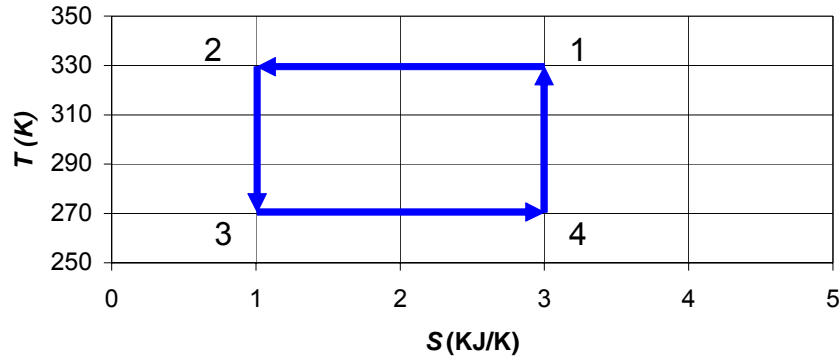
4→1 is isentropic (adiabatic and reversible) compression, the work input process.  $W_{4\rightarrow1}$  cannot be inferred from the T-S diagram.

For the Carnot heat engine cycle, net heat transfer,  $Q_{\text{net}}$ , is the area 1-2-3-4 or  $Q_{\text{net}} = (T_1-T_4)(s_2-s_1)$  (will be positive), and by the 1<sup>st</sup> Law for cycles:  $Q_{\text{net}} = W_{\text{net}}$

By Clausius' principle, the entropy generated in a Carnot heat engine cycle is zero, which can be shown using the T-S diagram above and noting that  $\Delta S = 0$  for a cycle:

$$S_{\text{gen}} = -\sum_k \left( \frac{Q}{T} \right)_k = -\frac{330(2)}{330} - \left( \frac{-270(2)}{270} \right) = 0$$

**(b) Carnot Refrigerator – all totally reversible processes**



1→2 is isothermal compression, the heat rejection process, and  $Q_H =$  area under line 1-2 or  $Q_H = T_1(s_2-s_1)$  (will be negative)

2→3 is isentropic (adiabatic and reversible) compression, the work input process.  $W_{2\rightarrow3}$  cannot be inferred from the T-S diagram.

3→4 is isothermal expansion, the heat input process, and  $Q_L =$  area under line 3-4 or  $Q_L = T_3(s_4-s_3)$  (will be positive and  $< Q_H$ )

4→1 is isentropic (adiabatic and reversible) expansion, the work output process.  $W_{4\rightarrow1}$  cannot be inferred from the T-S diagram.

For the Carnot refrigeration cycle, net heat transfer,  $Q_{net}$ , is the area 1-2-3-4 or  $Q_{net} = (T_1-T_4)(s_2-s_1)$  (will be negative), and by the 1<sup>st</sup> Law for cycles:  $Q_{net} = W_{net}$

By Clausius' principle, the entropy generated in a Carnot refrigeration cycle is zero, which can be shown using the T-S diagram above and noting that  $\Delta S = 0$  for a cycle:

$$S_{gen} = -\sum_k \left( \frac{Q}{T} \right)_k = -\left( \frac{-330(2)}{330} \right) - \left( \frac{270(2)}{270} \right) = 0$$